The **ECONOMICS OF PRODUCTION**

*by Bruce R. Beattie, C. Robert Taylor, & Myles J. Watts*


The Economics of Production is intended to serve as a textbook for courses in production economics theory—aimed at first-year graduate students and advanced undergraduates in economics, agricultural economics, and management. Technical aspects of production and input-side issues are given equal attention with the common notions of production costs, product supply, and other output-side issues found in most microeconomic theory texts. Given the authors’ informal writing style and penchant for detailed development of mathematical derivations, the result is a reader friendly product with ample intuitive motivation and concern for empirical application.

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